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FATIGUE LIFE PREDICTION IN THICK-WALLED CYLINDERS WITH COMPLEX RESIDUAL STRESSES

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) The large variation in stress intensity factors corresponding to various material models for a single, radial, straight-fronted crack in a pressurized, partially autofrettaged cylinder leads to a drastic difference in the fatigue life predictions. None of the predicted lives agree with experimental results. Possible explanations of the discrepancy are given and corresponding correction factors are introduced. The predicted lives based on the corrected stress intensity ranges are reasonably close to a set of well-documented experimental results of Throop and Fujczak. (Keywords)		

TABLE OF CONTENTS

	<u>Page</u>
ACKNOWLEDGEMENT	ii
INTRODUCTION	1
FATIGUE LIFE PREDICTION	2
SHAPE FACTORS	4
NEGATIVE K FACTOR F_N	5
LABORATORY SPECIMENS AND MEASURED LIVES	7
PREDICTED LIVES FOR THE EXPERIMENTS	8
CONCLUSIONS	10
REFERENCES	11

TABLES

I. VALUES OF f_{Sp} AND f_{SR} FOR DIFFERENT CRACK GEOMETRIES	10
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LIST OF ILLUSTRATIONS

1. Effect of reverse yielding on fatigue crack growth shown in a (α versus N/C_0) plot for a 2.0 diameter ratio cylinder with a single, straight-fronted through crack.	12
2. A schematic diagram of a cylinder specimen with initial 20-inch long notch and the growth of the notch by repeated pressurization.	13
3. Crack depth plotted versus number of fatigue loadings - experimental results.	14
4. Crack depth versus fatigue cycles for long curved cracks. Dots: experimental results, lines: calculated results.	15
5. Crack depth versus fatigue cycles for semi-elliptical cracks. Dots: experimental results, lines: calculated results.	16
6. Crack depth versus fatigue cycles for semi-circular cracks. Dots: experimental results, lines: calculated results.	17
7. Effect on fatigue cycles of various correction factors for a semi-elliptical surface crack in a pressurized, 60 percent autofrettaged cylinder.	18



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INTRODUCTION

Both finite element and modified mapping collocation methods have been used to obtain accurate stress intensity (K) solutions for pressurized autofrettaged thick cylinders with radial cracks (refs 1,2). Use of the weight function method has extended two-dimensional K solutions to more refined material models including reverse yielding caused by the Bauschinger effect (ref 3). Several papers have used stress intensity factors to estimate fatigue lives of cannon tubes (refs 4-6). The calculations underestimate the measured lives for pressurized cylinders, while they overestimate the experimental results for pressurized and autofrettaged cylinders (ref 5). The disagreement between measured and calculated lives diminishes in Reference 6 by introducing a fraction of the negative portion of K values as a part of the K range.

The shallow crack approximations for K solutions were used and a linear approximation for Bauschinger effect on residual hoop stress was assumed in References 5 and 6. The accurate two-dimensional K solutions affected by a significant Bauschinger effect using elastic-plastic analysis were used in Reference 7 to indicate the drastic effect of reverse yielding on the life prediction. Neither shape factors nor a fraction of negative K were considered in Reference 7.

In this report the life prediction formula similar to that used in Reference 7 is employed to check the calculated lives with experimental results of Throop (ref 8) and Throop and Fijczak (ref 9). The stress intensity factors for surface cracks of elliptical shape are approximated by the

References are listed at the end of this report.

two-dimensional stress intensity factors obtained in Reference 3 multiplied by respective shape factors for pressure and for residual stress given in Reference 5. The fraction of negative K included in K range varies from one at the notch boundary to zero at a crack depth far away from the notch. The variation of this fraction is assumed to be $1/r^2$ where r is the distance between the fatigue crack front and the notch front. Another modification is to use an initial crack depth much deeper than the notch depth. This is to avoid large cycles required in experiments to initiate a single continuous crack front along the notch boundary (it is considered likely (ref 5) that multiple, small, semi-elliptical cracks are initiated along the notch boundary prior to their link together to form a single crack). With these modifications the calculated lives agree reasonably well with experimental results for all three crack shapes: long curves, semi-elliptical, and semi-circular used in References 8 and 9.

FATIGUE LIFE PREDICTION

Integration of the Paris formula

$$\frac{da}{dN} = C(\Delta K)^m \quad (1)$$

for fatigue growth rate of a crack subjected to cyclic loading is usually used to determine the number of fatigue cycles required to grow a crack from an initial depth a_i to a final depth a_f .

$$N = N_f - N_i = \int_{a_i}^{a_f} \frac{da}{C(\Delta K)^m} \quad (2)$$

where C and m are material constants and ΔK is the range of stress intensity defined by

$$\Delta K = K_{\max} - K_{\min} \quad (3)$$

K_{\max} and K_{\min} are maximum and minimum values of K in a loading cycle. Assume that a crack face is a geometric plane and there is no possibility of interpenetration under compression. This leads to a conclusion that K_{\min} cannot be a negative value. In the case of repeated firing of cannon tubes

$$K_{\min} = 0 \quad (4)$$

is used for both autofrettaged and nonautofrettaged tubes. If K_p and K_R denote mode I K values corresponding to an internal pressure and a residual hoop stress respectively, then

$$K_{\max} = K_p \quad (5a)$$

for nonautofrettaged cylinders, and

$$K_{\max} = K_p + K_R \quad (5b)$$

for autofrettaged cylinders. K_p and K_R are usually expressed in a dimensionless form denoted by f_{Kp} and f_{KR} , respectively,

$$f_{Kp} = \frac{K_p}{p\sqrt{\pi a}}, \quad f_{KR} = \frac{K_R}{\sigma_0\sqrt{\pi a}} \quad (6)$$

where σ_0 is the yield stress, p is the internal pressure applied to a tube, and p is related to σ_0 by a load factor $f_L = \sigma_0/p$. By virtue of Eqs. (3), (4), and (5b)

$$\Delta K = \left(\frac{f_{Kp}}{f_L} + f_{KR} \right) \sigma_0 \sqrt{\pi a} \quad (7)$$

For a small crack growth from a_j to a_{j+1} , f_{Kp} and f_{KR} are assumed to be constants which are taken as the mean values

$$\begin{aligned} \bar{f}_{Kp} &= \frac{1}{2}(f_{Kp}(a_j) + f_{Kp}(a_{j+1})) \\ \bar{f}_{KR} &= \frac{1}{2}(f_{KR}(a_j) + f_{KR}(a_{j+1})) \end{aligned} \quad (8)$$

The integration of Eq. (2) becomes

$$\frac{N}{C_0} = \frac{N_f - N_i}{C_0} = \sum_{j=1}^n 2^{-m} \left(\frac{\bar{f}_{KP}}{\bar{f}_L} + \bar{f}_{KR} \right)^{-m} (\alpha_j^{1-m/2} - \alpha_{j+1}^{1-m/2}) \quad (9)$$

where

$$C_0 = \frac{2}{C(m-2)} \left(\frac{\sigma_0 \sqrt{\pi}}{2} \right)^{-m} (t)^{1-m/2} \quad (10)$$

with t denoting the wall thickness and $\alpha = a/t$. The fraction α is used since the crack depth is usually expressed as a fraction of wall thickness t .

Substituting from calculated values of \bar{f}_{KP} and \bar{f}_{KR} (ref 3) corresponding to various material models in Eqs. (8) and (9), we obtain the fatigue crack growth (α versus N/C_0) graph shown in Figure 1 for a single, two-dimensional straight-fronted through crack in a cylinder of diameter ratio two. In this figure, f is the Bauschinger effect factor. The dotted lines are for idealized material without Bauschinger effect ($f = 1$), while the dashed lines are for $f = 0.38$ (100 percent overstrain) and $f = 0.44$ (60 percent overstrain), respectively. The dashed lines with $m' = 0$ correspond to elastic-perfectly plastic behavior during reverse yielding. The dashed lines with $m' = 0.3$ indicate the difference in predicted cycles when strain-hardening is considered in reverse yielding. The graph shows the significant difference of autofrettage effect of various material models on fatigue cycles. Such a drastic difference is not supported by experimental results. Corrective parameters must be introduced to correlate the calculated fatigue cycles with observed ones in laboratory tests.

SHAPE FACTORS

The ratio of stress intensity factor for a surface crack to that of a two-dimensional through crack is called the shape factor. The stress intensity factor varies along the crack front of a surface crack. It changes with

crack shape and under different loadings. If the variation of stress intensity along the crack front is important, the three-dimensional K solutions for the surface crack should be obtained. If an estimate of K at a point, say the deepest point of the surface crack, is needed, then a reasonable estimate of shape factor is useful. An extensive study of shape factors has been published by Newman and Raju (ref 10) for semi-elliptical cracks in a flat plate under tension or bending. There is no comparable study for such a crack in a thick cylinder. Parker et al (ref 5) obtained estimates of shape factors for semi-elliptical cracks of various aspect ratios in a pressurized and autofrettaged cylinder from judicious use of results reported in Reference 10. More accurate three-dimensional K solutions should be obtained to check these estimates. Before more accurate and reliable shape factors become available, values close to those given by (a) and (c) of Figure 7 in Reference 5 are used for f_{sp} and f_{SR} , respectively, in this study. Multiplying f_{Kp} and f_{KR} with their shape factors, Eq. (7) becomes

$$\Delta K = \left(\frac{f_{Sp} f_{Kp}}{f_L} + f_{SR} f_{KR} \right) \sigma_0 \sqrt{\pi a} \quad (11)$$

The following mean values are used in Eq. (11) for a small crack growth from a_j to a_{j+1} .

$$\begin{aligned} \overline{f_{Sp} f_{Kp}} &= \frac{1}{2} [f_{Sp}(a_j) f_{Kp}(a_j) + f_{Sp}(a_{j+1}) f_{Kp}(a_{j+1})] \\ \overline{f_{SR} f_{KR}} &= \frac{1}{2} [f_{SR}(a_j) f_{KR}(a_j) + f_{SR}(a_{j+1}) f_{KR}(a_{j+1})] \end{aligned} \quad (12)$$

NEGATIVE K FACTOR F_N

For a fatigue crack which is considered as a geometrical plane with no thickness, $K_{min} = 0$ is used in Eq. (3) to obtain K range. For a notch with finite thickness, the upper and lower planes of the notch may have normal

displacement in both directions. The argument used to limit $K_{min} = 0$ is not valid at the notch front. In fact, the full negative K should be used for a crack starting at the notch. At some depth, the notch effect may become negligibly small, and $K_{min} = 0$ may again be used in Eq. (3) for ΔK . Kendall has argued that a portion of the negative K must be included in calculating K range (ref 6). He introduced a constant fraction which is multiplied by the negative K (K_R) corresponding to compressive residual stress due to autofretage to give the K_{min} in ΔK . From our hypothesis, the fraction varies with the depth of the fatigue crack. As a first approximation, the fraction f_N is taken as $(1 + r/r_n)^{-2}$ where r_n is the depth of the notch and r is the depth of the crack measured from the notch front. At the notch front $r = 0$ and $f_N = 1$, the full negative K is taken as K_{min} . When $r = r_n$ the fatigue crack grows to a depth equal to the notch depth; this approximation gives $f_N = 1/4$. It is also assumed that $f_N = 0$ when $r > 2r_n$. A linear variation of f_N was another approximation examined which underestimated the measured fatigue lives. Incorporating f_N , Eq. (11) becomes

$$\Delta K = [f_{Sp} \frac{\bar{f}_{Kp}}{\bar{f}_L} + (1-f_N)f_{SR}f_{KR}] \sigma_o \sqrt{\pi a} \quad (13)$$

Equation (9) can be expressed explicitly

$$\frac{N}{C_o} = \sum_{j=1}^n \left[\frac{\bar{f}_{Kp}(a_j) + \bar{f}_{Kp}(a_{j+1})}{\bar{f}_L} + \bar{f}_{KR}(a_j) + \bar{f}_{KR}(a_{j+1}) \right]^{-m} (a_j^{1-m/2} - a_{j+1}^{1-m/2}) \quad (14)$$

where abbreviations \bar{f}_{Kp} , \bar{f}_{KR} are

$$\begin{aligned} \bar{f}_{Kp}(a_j) &= f_{Sp}(a_j) f_{Kp}(a_j) \\ \bar{f}_{KR}(a_j) &= [1 - f_N(a_j)] f_{SR}(a_j) f_{KR}(a_j) \end{aligned} \quad (15)$$

LABORATORY SPECIMENS AND MEASURED LIVES

Throop (ref 8) and Throop and Fuczak (ref 9) obtained a series of experimental results which relate fatigue crack lives with crack shape and extent of autofrettage for thick-wall cylinders. The cylinders were 0.76 m (30 inches) in length, 180 mm (7.1 inches) bore diameter, 360 mm (14.25 inches) outside diameter and were fatigue cracked from longitudinal internal notches. Three initial notch geometries were used; semi-circular, 100 mm (4-inch) and 500 mm (20-inch) long notches produced by electrical discharging machining. They were 6.4 mm ($\frac{1}{4}$ -inch) deep by 0.76 mm (0.03-inch) wide, the semi-circular notch being 13 mm ($\frac{1}{2}$ -inch) diameter half-penny shape. Fatigue cracks grown from the initial notches were monitored periodically for depth and shape with ultrasonics as the cylinder was repeatedly pressurized to 330 MPa (48 Ksi). The cylinder material was ASTM A723 forged steel, with yield strength of 1175 MPa, -40°C Charpy impact energy of 34 J, reduction in area of 50 percent. A schematic diagram of a typical cylinder with a simple initial notch and the growth of a 500 mm (20-inch) long notch from 6.4 mm ($\frac{1}{4}$ -inch) initial depth by repeated pressurization is shown in Figure 2. The measured crack depth versus corresponding number of fatigue loadings is shown in Figure 3 for a single-notched cylinder with 0, 30, and 60 percent overstrains for three-notch geometries.

Since the fatigue crack is not likely to start from the notch immediately, an adjustment of experimental results is made by subtracting the number of cycles required to grow from initial notch depth to an initial crack depth (a_i) from the number of cycles to grow from initial notch depth to a final crack depth (a_f). The initial crack depth, which should be reasonably

larger than the initial notch depth (6.4 mm in this experimental study), is arbitrarily taken as $a_i = 0.1t = 9$ mm. The original experimental data are available only in graphs. To improve the accuracy of readings from graphs, the graphs were first enlarged and the average was used from values obtained from different graphs published in different papers (refs 4,5,9) for the same set of experimental data. The adjusted experimental results are shown by dots in Figures 4, 5, 6, and 7.

PREDICTED LIVES FOR THE EXPERIMENTS

The material constants for the steel used in the experiments are $m = 3$ and $C = 6.52 \times 10^{-12}$ for crack growth in meters per cycle and ΔK in $\text{MPa}\sqrt{\text{meter}}$ (or $C = 3.4 \times 10^{-10}$ for crack growth in inches per cycle and ΔK in $\text{Ksi}\sqrt{\text{inch}}$). Using $f_L = 3.55$ and values of f_{Sp} and f_{SR} in Table I, and assuming $f_N = (1 + r/r_N)^{-2}$ for $0 < r < 2r_N$ and $f_N = 0$ for $r > 2r_N$, Eqs. (14) and (15) can be evaluated with known discrete values of f_{Kp} and f_{KR} . Values of f_{Sp} and f_{SR} , given in Table I, are obtained from Reference 5 for different crack geometries. Discrete values of f_{Kp} and f_{KR} can be computed by the method described in Reference 3. The calculated lives and measured lives are plotted in Figures 4, 5, and 6 for three crack geometries, respectively. For nonautofrettaged cylinders (zero percent overstrain), there is only one set of calculated results, shown in a solid line, for each crack configuration. For 60 percent overstrain, solid lines are for idealized material without considering the Bauschinger effect, while two dashed lines in each figure are predicted lives with some reverse yielding. The two dashed lines differ in m' values, $m' = 0$ or 0.3 , where $m'E$ is the slope of strain-hardening during reverse yielding.

When $m' = 0$, the material behaves like elastic-perfectly plastic in reverse yielding. The magnitude of the compressive, residual stress in the tangential direction near the bore is smaller than that in a strain-hardening material (ref 3). The strain-hardening reduces the adverse effect of reverse yielding due to the Bauschinger effect, Figure 1. Figures 4 through 6 show an overall effect of all factors. Figure 7 shows the effect of each factor on the semi-elliptical surface crack in a pressurized cylinder with 60 percent overstrain. The dotted curve, curve 1, gives the calculated lives for an idealized material with no Bauschinger effect. No correction factors are used. The stress intensity range is based on two-dimensional stress intensity factors and $K_{min} = 0$. If the change in residual hoop stress due to the Bauschinger effect (Bauschinger effect factor $f = 0.44$) is considered, the calculated lives are shown as a dashed curve, curve 2, where $m' = 0.3$ is used. The large difference between curves 1 and 2 shows the significant effect of reverse yielding on fatigue lives. If shape factors f_{Sp} and f_{SR} are considered in addition to the Bauschinger effect, the predicted lives will be changed from curve 2 to curve 3. The shape factors are to increase the fatigue lives. Finally, if the correction factor f_N is also taken into consideration, the predicted lives are shown as the solid line, curve 4, which is close to the experimental results shown by dots in Figure 7. Similar graphs, obtained for the long curved crack and the semi-circular crack, are omitted since they indicate similar effects of each correction factor.

TABLE I. VALUES OF f_{Sp} AND f_{SR} FOR DIFFERENT CRACK GEOMETRIES

$\alpha = a/t$	20-Inch Long Notch		4-Inch Long Notch		Semi-Circular Notch	
	f_{Sp}	f_{SR}	f_{Sp}	f_{SR}	f_{Sp}	f_{SR}
0.1	0.95	0.95	0.72	0.69	0.57	0.58
0.2	0.90	0.90	0.64	0.60	0.53	0.52
0.3	0.85	0.85	0.61	0.55	0.51	0.42
0.4	0.85	0.80	0.57	0.47	0.48	0.34
0.5	0.85	0.75	0.56	0.38	0.44	0.24

CONCLUSIONS

The fatigue life of a thick-walled cylinder can be predicted reasonably well by integration of the Paris formula for growth rate of a fatigue crack under cyclic loading, if a modified stress intensity range is used. The stress intensity range is obtained by multiplying two-dimensional stress intensity factors by proper shape factors and some negative K factors. More systematic and controlled experiments are required to check the idea proposed in this report. Three-dimensional K solutions for semi-elliptical surface cracks in thick cylinders with various residual stresses are needed to estimate the proper shape factors. Special experiments should be performed to verify the concept of negative K factors and to determine the variation of f_N in terms of crack depth.

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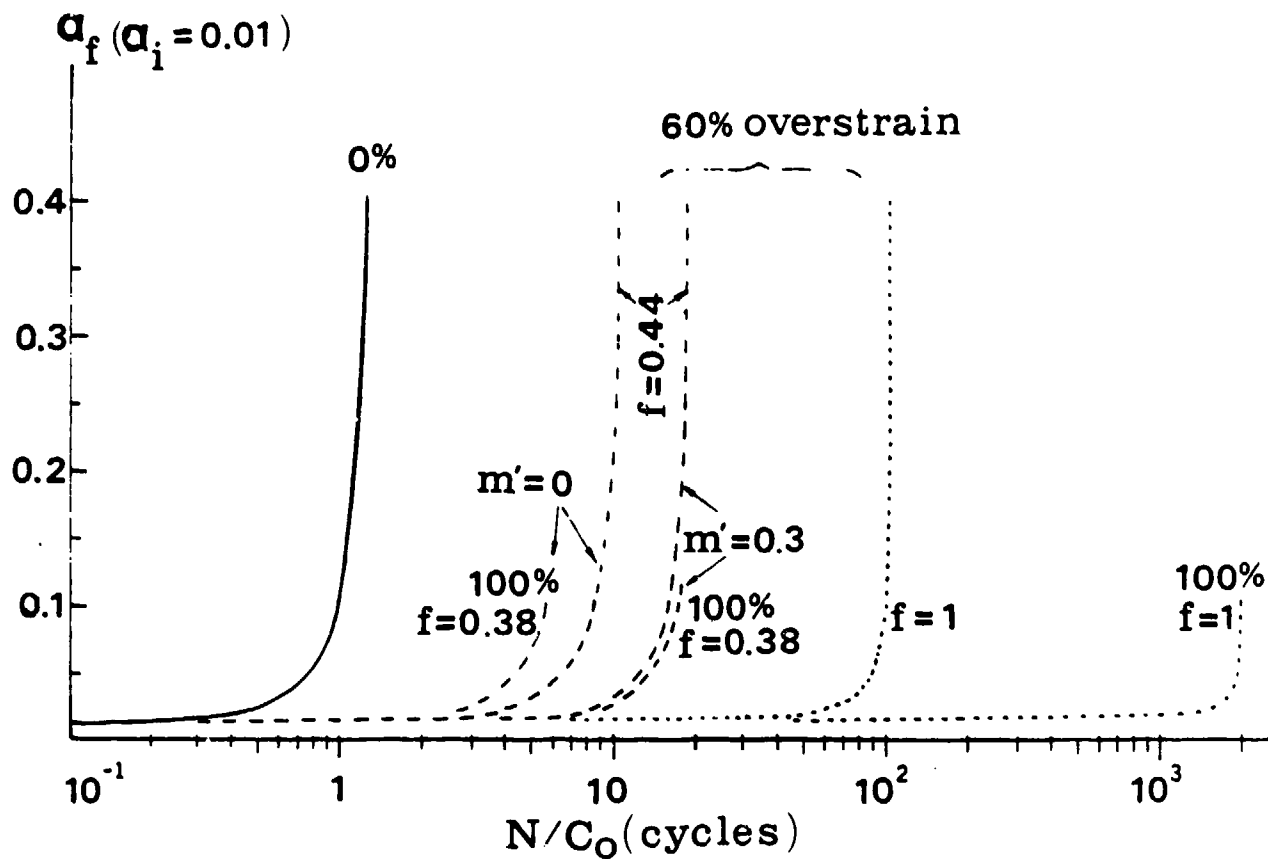


Figure 1. Effect of reverse yielding on fatigue crack growth shown in a (a versus N/C_0) plot for a 2.0 diameter ratio cylinder with a single, straight-fronted through crack.

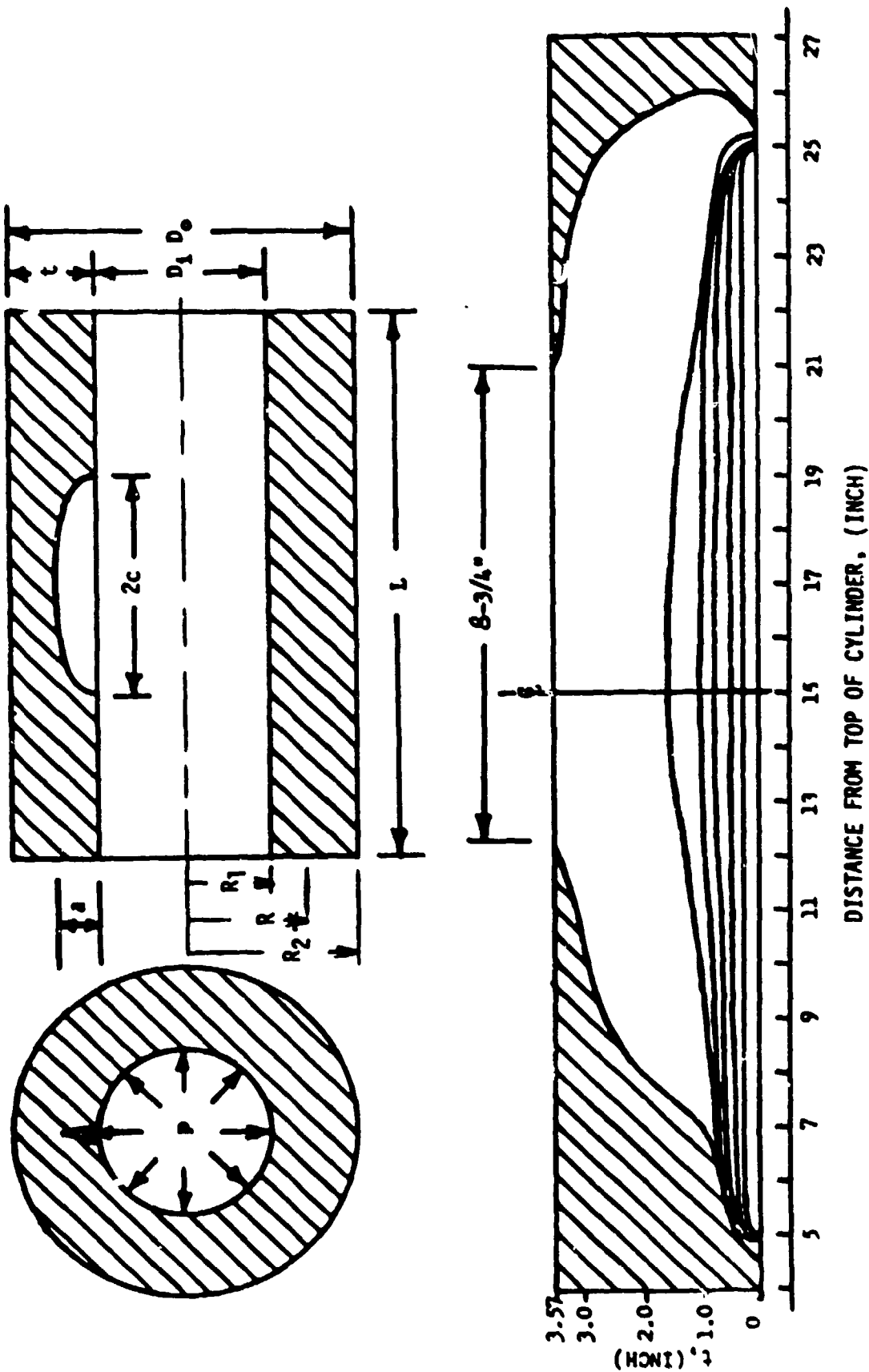
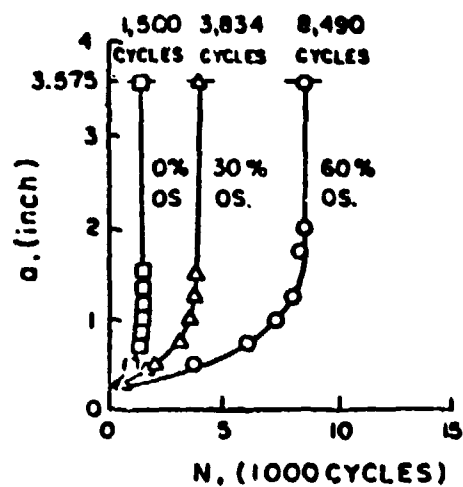
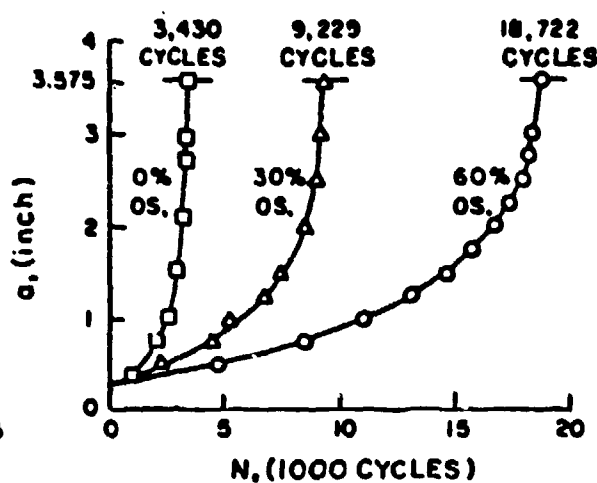


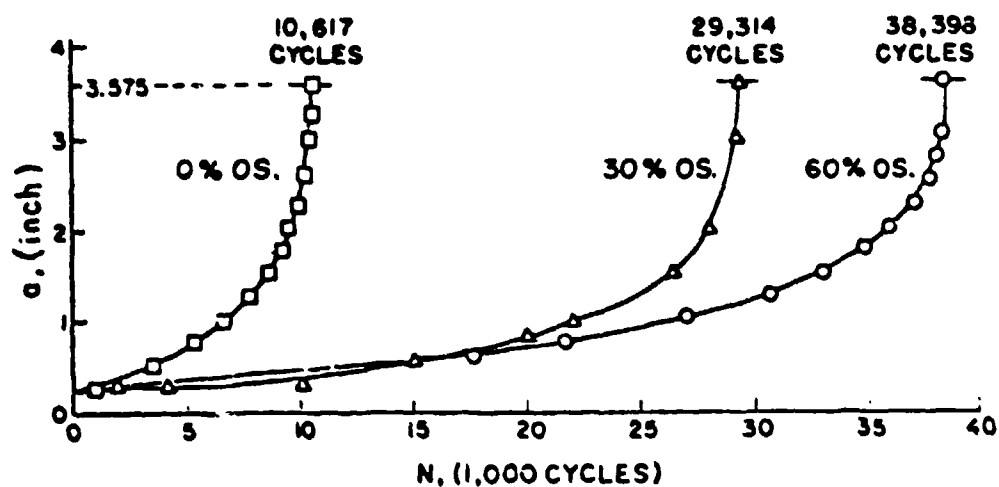
Figure 2. A schematic diagram of a cylinder specimen with initial 20-inch long notch and the growth of the notch by repeated pressurization (ref 9).



(a) LONG CURVED CRACK



(b) SEMI-ELLIPTICAL CRACK



(c) SEMI-CIRCULAR CRACK

Figure 3. Crack depth plotted versus number of fatigue loadings - experimental results (ref 9).

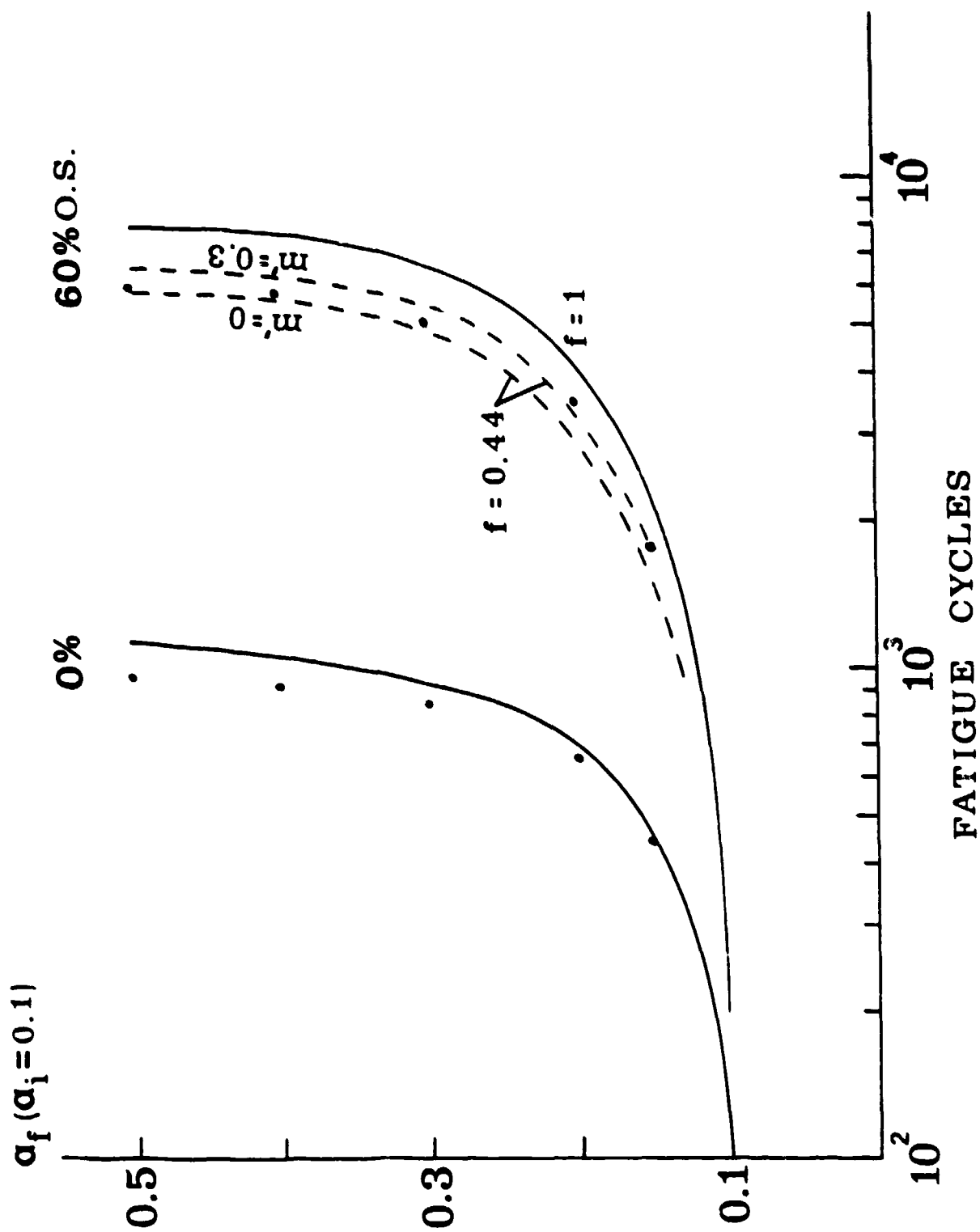


Figure 4. Crack depth versus fatigue cycles for long curved cracks.
Dots: experimental results, lines: calculated results.

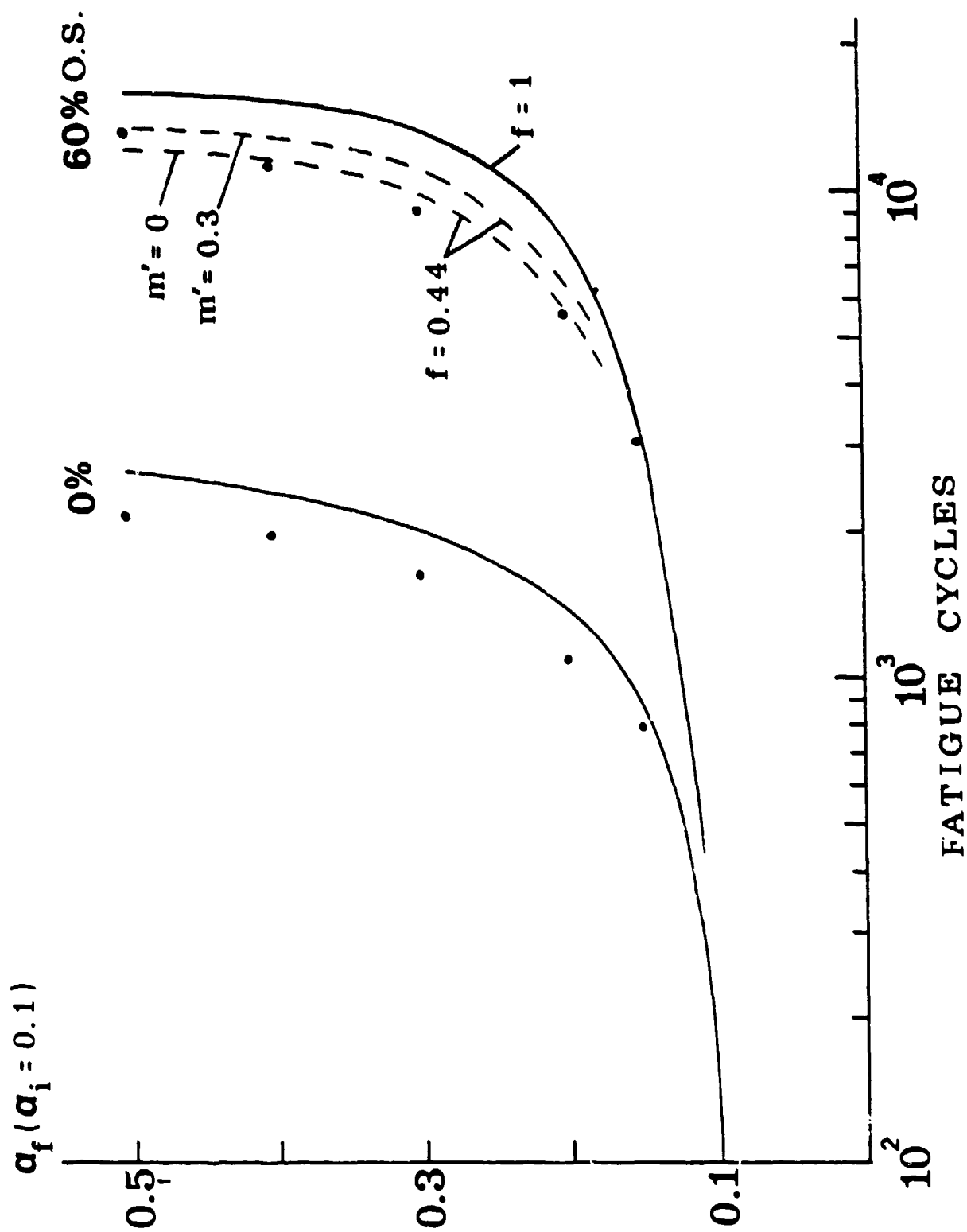


Figure 5. Crack depth versus fatigue cycles for semi-elliptical cracks.
Dots: experimental results, lines: calculated results.

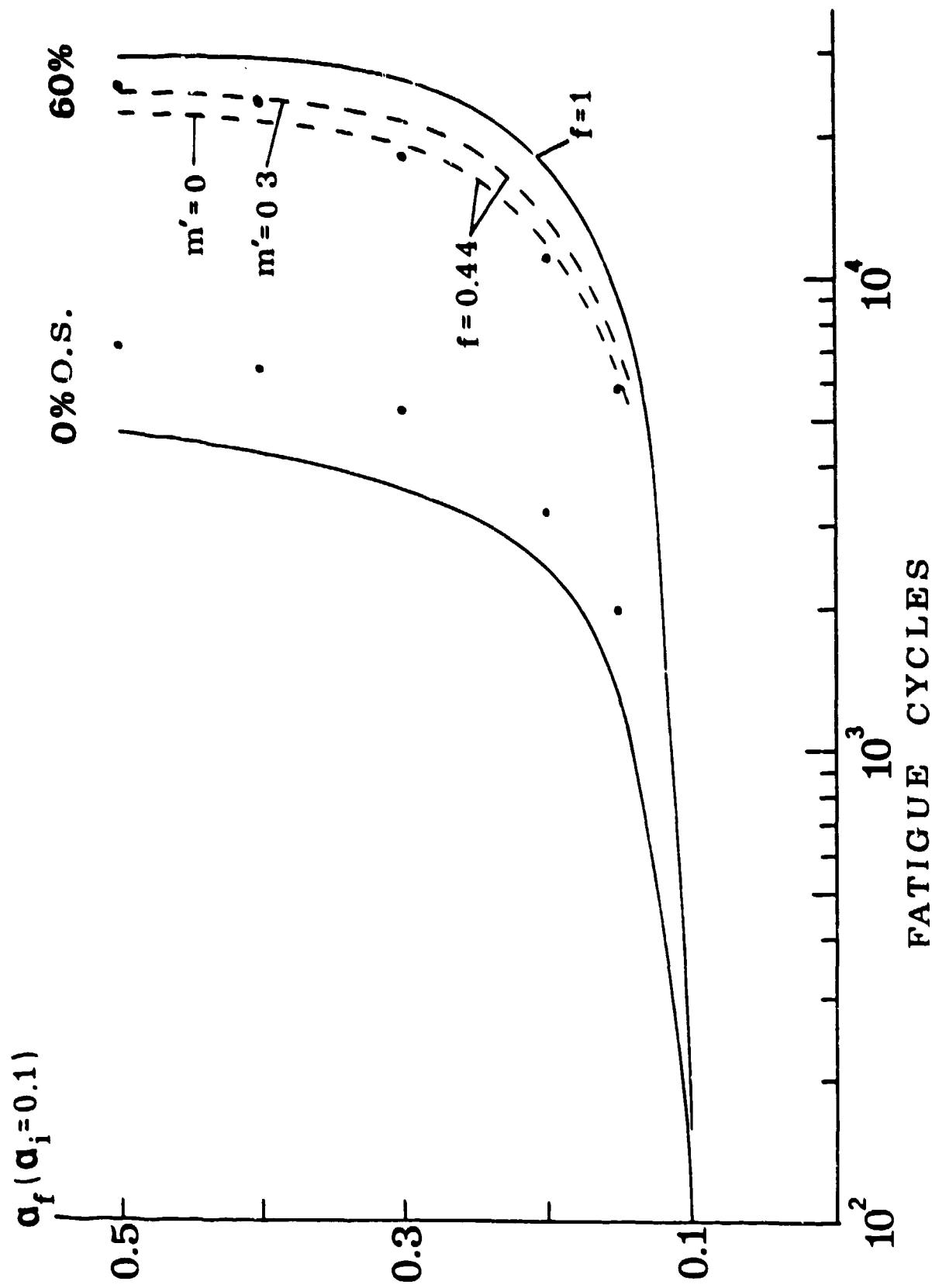


Figure 6. Crack depth versus fatigue cycles for semi-circular cracks.
Dots: experimental results, lines: calculated results.

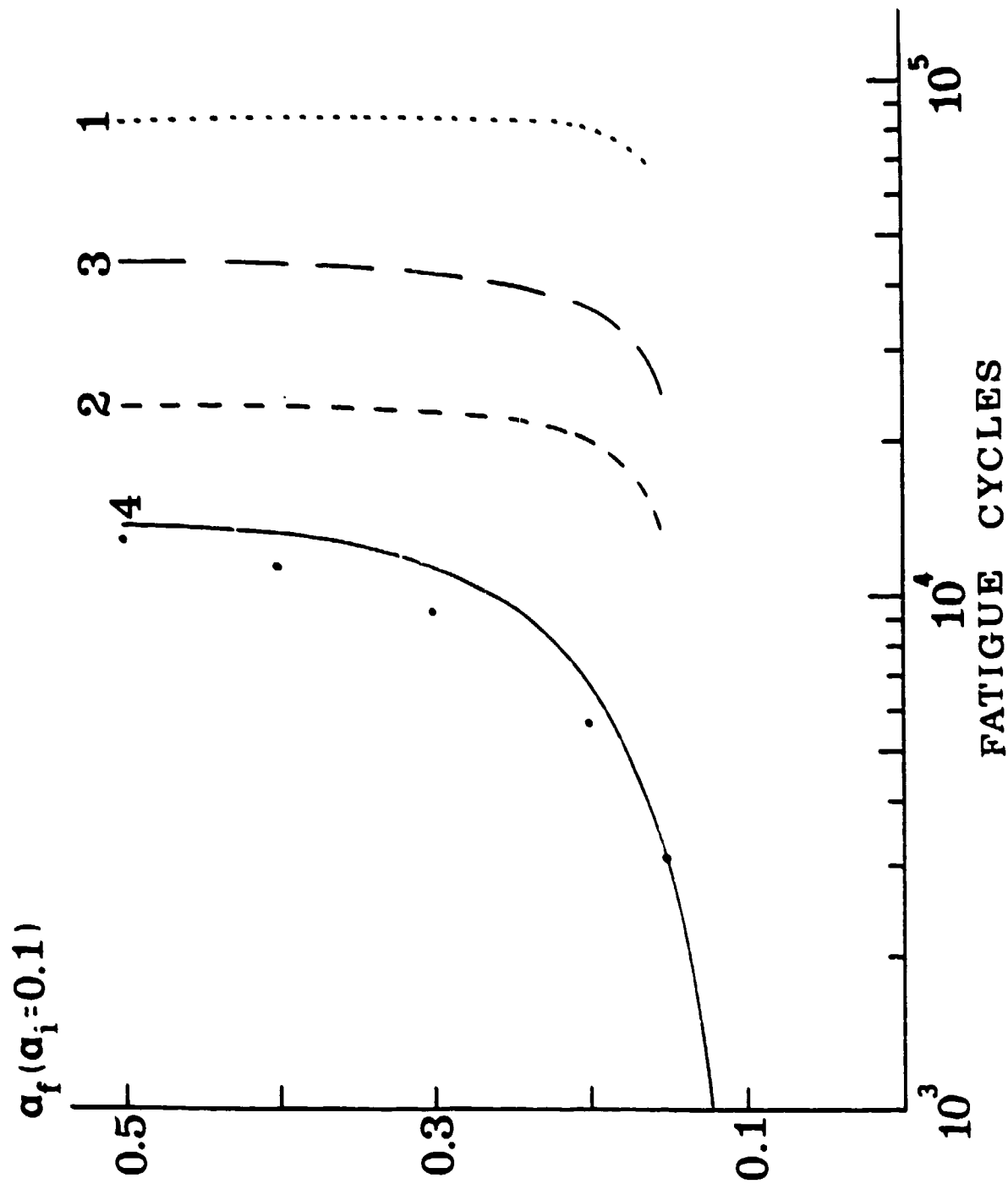


Figure 7. Effect on fatigue cycles of various correction factors for a semi-elliptical surface crack in a pressurized, 60 percent autofrettaged cylinder.

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